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BOREHOLE SURVEYING

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1 "Borehole Surveying" 2 This invention relates to a method and apparatus for use in surveying of boreholes. 5 6 It is known in directional drilling, for example, to 7 detect the orientation of a drillstring adjacent to 8 the bit by means of a sensor package for determining 9 the local gravitational [GX,GY,GZ] and magnetic [BX,BY,BZ] field components along mutually 10 orthogonal axes, and to derive from these the local 11 azimuth (AZ) and inclination (INC) of the 12 drillstring. Conventionally, the measurements are 13 made by providing within the instrument package 14 15 three mutually perpendicular accelerometers and three mutually perpendicular magnetic fluxgates. 16 17 18 The present invention is concerned with an arrangement which requires only two measurement 19 20 devices, namely a single accelerometer and a single 21 magnetic fluxgate or a single accelerometer and a 22 single rate gyro, the latter being preferred for situations in which magnetic interference is likely 23 24 to be encountered. 25 26 Accordingly, the present invention provides a method of surveying boreholes, comprising: 27

providing an instrument package in the leading 1 end of a drillstring, the instrument package 2 comprising first and second single-axis sensors 3 mounted for rotation with the drillstring about the 4 rotational axis of the drillstring, the first sensor 5 being an accelerometer and the second sensor being a 6 magnetic fluxgate or a rate gyro; 7 rotating the drillstring; 8 deriving from the first sensor the inclination 9 angle of the drillstring at the instrument package; 10 and 11 deriving from the second sensor the azimuth 12 angle of the drillstring at the instrument package. 13 14 Each of the sensors will typically be positioned in 15 one of two configurations. In the first 16 configuration, the sensor is radially spaced from 17 the borehole axis and has its sensing axis in a 18 plane containing the borehole axis and an axis 19 perpendicular thereto. In the second configuration, 20 the sensor is radially spaced from the borehole axis 21 and has its sensing axis in a plane parallel with 2.2. the borehole axis. 23 24 Preferably, the drilling control rotation angle is 25 also obtained from the sensor outputs. 26 27 Preferably, the sensor outputs are integrated over 28 the four quadrants of rotation and the desired 29 output angle is derived from the integrated output. 30 The instrument package suitably includes rotation 31 angle reference means for use in the integration. 32

1 2 Additional information may be derived, such as the local gravitational and magnetic field vectors. 3 4 From another aspect, the invention provides 5 apparatus for use in surveying boreholes, the 6 7 apparatus comprising an instrument package adapted to be included in the leading end of a drillstring, 8 the instrument package comprising first and second 9 single-axis sensors mounted for rotation with the 10 11 drillstring about the rotational axis of the drillstring, the first sensor being an accelerometer 12 13 and the second sensor being a magnetic fluxgate or a rate gyro; and computing means for deriving from the 14 15 first sensor while the drillstring is rotating the inclination angle of the drillstring at the 16 instrument package, and for deriving from the second 17 18 sensor while the drillstring is rotating the azimuth 19 angle of the drillstring at the instrument package. 20 21 The computing means preferably operates to integrate 22 the sensor outputs over the four quadrants of 23 rotation and to derive the desired output angle 24 from the integrated output. 25 26 The apparatus may further include rotation angle 27 reference means for use in the integration. 28 29 Examples of the present invention will now be 30 described, by way of illustration only, with 31 reference to the drawings, in which:

Fig. 1 illustrates, in general terms, the 1 operation of a single axis sensor in a drillstring 2 for sensing any given vector V; 3 Fig. 2 is a block diagram of one circuit which 4 may be used to identify rotation quadrant; 5 Fig. 3 illustrates the operation where the 6 sensor is an accelerometer; 7 Fig. 4 illustrates the operation where the 8 sensor is a fluxgate; 9 Fig. 5 illustrates the derivation of azimuth 10 angle; and 11 Fig. 6 illustrates the operation where the 12 sensor is a rate gyro. 13 14 15 Single-axis sensor 16 17 The operation of a single-axis sensor in a drill 18 string will first be described in general terms. 19 The application of this to specific sensors is 20 discussed below. 21 22 Referring to Fig. 1, a single-axis sensor 10 is 23 mounted on a drill string (not shown). The sensor 24 10 senses a fixed vector {V} and is mounted in one 2.5 of two configurations. 26 27 In the first configuration, the sensor 10 lies in a 28 plane containing the rotation axis (OZ) of the drill 29 string and axis (OX) perpendicular to (OZ). Axis 30 (OY) makes up the conventional orthogonal set of 31 axes [OX,OY,OZ]. The sensor 10 is mounted at a 32

```
distance r from the (OZ) axis and the angle between
      the sensing axis (OS) and the rotational axis (OZ)
 2
      is m.
 3
 4
      In the second configuration, the sensor 10 is
 5
      mounted in a plane which is parallel to the borehole
6
      axis (OZ) and with its sensing axis perpendicular to
7
      the axis (OY) and making angle m with the direction
9
      of the borehole axis (OZ).
10
      If the rate of rotation about the (OZ) axis is w and
11
12
      the components of {V} are {VOZ} along the (OZ) axis
      direction and {VOXY} in the (OXY) plane, then if the
13
14
      output from the sensor 10 for both configuration 1
15
      and configuration 2 of Figure 1 is of the form
16
17
      V(t) = VOZ.cos(m) + VOXY.sin(m).cos(w.t) + c
18
      where time t = 0 when the axis (OX) is coincident
19
20
      with the direction of \{VOXY\} and c is constant for
21
      any fixed rotation rate w.
22
23
      Thus, the sensor output at time t can be written:
24
25
      V(t) = K1.cos(w.t) + K2
26
      where K1 = VOXY.sin(m) and K2 = VOZ.cos(m) + c are
27
      constant if the vector amplitudes VOZ and VOXY are
28
29
      constant.
```

```
Sensor output integration
1
2.
     The integration of V(t) from any initial time ti to
3
      ti + T/4, where T = 2.\pi/w, the time for one
4
      revolution about (OZ), is
5
6
      Q = \int_{ti}^{ti+T/4} K1.\cos(wt).dt + \int_{ti}^{ti+T/4} K2.dt
7
8
9
      Thus,
                            ti + T/4
10
                                        + K2.T/4
      Q = [(K1/w).sin(w.t)]
11
                             ti
12
13
14
      or
15
      Q = (K1/w).[\sin(w.ti + w.T/4) - \sin(w.ti)] + L
16
17
18
      or
      Q = (K1/w).[\sin(w.ti + \pi/2) - \sin(w.ti)] + L
19
20
      or
      Q = (K1/w).[cos(w.ti) - sin(w.ti)] + L \qquad ....(ii)
21
      where L is a constant = K2.T/4.
22
23
      Using equation (ii), the integration of V(t) from an
24
      arbitrary time t0 to time t0+T/4 yields
25
26
       Q1 = (K1/w).[\cos(w.to) - \sin(w.to)] + L \qquad \dots (iii)
27
28
       Using equation (ii), the integration of V(t) from
29
       time t0+T/4 to time t0+T/2 yields
30
31
```

```
O2 = (K1/w).[cos(w.t0 + w.T/4) - sin(w.t0 + w.T/4)]+L
1
2
      Q2 = (K1/w) \cdot [\cos(w.t0 + \pi/2) - \sin(w.t0 + \pi/2)] + L
3
4
      O2 = (K1/w).[-sin(w.t0) - cos(w.t0)] + L ...(iv)
5
6
      Using equation (ii), the integration of V(t) from
7
8
      time t0+T/2 to t0+3T/4 yields
9
      O3 = (K1/w) \cdot [\cos(w \cdot t0 + w \cdot T/2) - \sin(w \cdot t0 + w \cdot T/2)] + L
10
11
      or
      Q3 = (K1/w) \cdot [\cos(w \cdot t0 + \pi) - \sin(w \cdot t0 + \pi)] + L
12
13
      or
      O3 = (K1/w) \cdot [-cos(w.t0) + sin(w.t0)] + L \dots (v)
14
15
       Using equation (ii), the integration of V(t) from
16
       time t0+3T/4 to time t0+T yields
17
18
       Q4 = (K1/w).[\cos(w.t0+w.3T/4) - \sin(w.t0+w.3T/4)]+L
19
20
       or
       Q4 = (K1/w) \cdot [\cos(w \cdot t0 + 3\pi/2) - \sin(w \cdot t0 + 3\pi/2)] + L
21
22
       or
       Q4 = K1/w).[sin(w.t0) + cos(w.t0)] + L ....(vi)
23
24
       Writing K = K1/w and \alpha = w.t0, then equations (iii)
25
       through (vi) yield for the four successive
26
       integrations of V(t)
27
28
                                                .....(vii)
       01 = -K.\sin\alpha + K.\cos\alpha + L
29
                                                 .....(viii)
       Q2 = -K.\sin\alpha - K.\cos\alpha + L
30
                                                  ....(ix)
       Q3 = K.\sin\alpha - K.\cos\alpha + L
31
```

1	$Q4 = K.\sin\alpha + K.\cos\alpha + L \qquad \dots (x)$
2	
3	Integration control
4	
5	In order to control the sensor output integration,
6	as just described, over four successive quarter
7	periods of the drill string rotation, a train of ${f n}$
8	(with ${f n}$ any multiple of 4) equally spaced pulses per
9	revolution must be generated. If one pulse $\mathbf{P_0}$ of
10	this pulse train is arbitrarily chosen at some time
11	t0, the repeated pulses $P_{n/4},\ P_{n/2}$ and $P_{3n/4}$ define
12	times $t0+T/4$, $t0+T/2$ and $t0+3T/4$ respectively where
13	the period of rotation $T = 2\pi/w$ and w is the angular
14	velocity of rotation.
15	
16	A suitable means for generating an appropriate
17	control pulse train is described in US-A1-
18	20020078745, which is hereby incorporated by
19	reference.
20	
21	In an alternative form of integration control, the
22	sensor output waveform itself can be used with
23	appropriate circuitry for defining the integration
24	quadrant periods. In particular, the relatively low
25	noise magnetic fluxgate output is well suited to act
26	as input to a phase-locked-loop arrangement. Fig. 2
27	shows such an arrangement, successive output pulses
28	defining the integration quadrants.
29	
30	Rotation angle

```
1
      Equations (vii) through (x) can be solved to yield
      angle \alpha; there is a degree of redundancy in the
 2
 3
      possible solutions but, for example,
 4
 5
      Q1 - Q2 = 2K.\cos\alpha
 6
      and
 7
      Q3 - Q2 = 2K.sin\alpha
 8
      or
      \sin\alpha/\cos\alpha = (Q3-Q2)/(Q1-Q2) \qquad \dots (xi)
 9
10
11
      Since \alpha = w.t0, the angle S(t0) between the axis
12
      (OX) and the direction of {VOXY} at time tO can be
13
      determined from equation (xi), and the angle between
14
      (OX) and {VOXY} at any time tm measured from the
15
      arbitrary starting time t0 is then
16
17
      S(tm) = \alpha + w.tm = S(t0) + 2\pi.tm/T ....(xii)
18
19
      Magnitudes of vectors {VOXY} and {VOZ}
20
21
      Equations (vii) through (x) can be solved to yield
22
      the constant L:
23
24
      L = (Q1 + Q2 + Q3 + Q4)/4 ..... (xiii)
25
26
      and the constant K can be determined from:
27
      (K)^2 = [(Q1-L)^2 + (Q2-L)^2]/2
28
                          = [(Q3-L)^2 + (Q4-L)^2]/2 ...(xiv)
29
30
```

The magnitude of vector {VOZ} can be determined as

```
1
2
     VOZ = (K2-c)/cos(m) = (4.L/T - c)/cos(m) ....(xv)
     provided that constant c is known.
3
4
     The magnitude of vector {VOXY} can be determined as
5
6
7
     VOXY = K1/\sin(m) = (K.w)/\sin(m) \qquad \dots (xvi)
8
9
     Inclination angle
10
11
     The inclination angle (INC) can be derived from the
     gravity vector {G} with the aid of a rotating
12
13
     accelerometer.
14
     Referring to Fig. 3, where (INC) is the angle
15
16
     between the tool axis (OZ) and the gravity vector
17
     {G},
18
19
     GOZ = G.cos(INC)
                                         ....(xvii)
20
     and
21
     GOXY = -Gsin(INC)
                                         ....(xviii)
22
23
     The accelerometer output can be written as
24
25
     VG(t) = GOZ.cos(m) + GOXY.sin(m).cos(wt)
26
                + CP.sin(m) + D.sin(m)
                                         .....(xix)
27
28
     where CP is a centripetal acceleration term and D is
29
     a sensor datum term. The centripetal acceleration
30
     term CP is zero for configuration 2 and makes this
31
     the preferred configuration for mounting of the
32
     accelerometer.
```

```
1
      Since CP is proportional to w^2/r and is constant for
2
      constant w, then clearly VG(t) is of the form
 3
 4
5
     VG(t) = K1.cos(w.t) + K2(w)
      (or K1.cos(w.t) + K2 for configuration 2) ....(xx)
6
8
     where K1 and K2(w) are constants at constant angular
     velocity \mathbf{w} in the case of configuration 1 and always
9
      constant in the case of configuration 2. the
10
      constants K1 and K2(w) can be determined from the
11
12
      accelerometer output integrations as described above
13
      together with the angle (Highside Angle HS = w.t)
14
      between the axis (OX) and the direction of {GOXY}.
15
16
     K1 = GOXY.sin(m)
                                      ....(xxi)
17
      and
18
      K2(w) = GOZ.cos(m) + D.sin(m)
                                       .....(xxii)
19
     with
20
      C(w) = CP.sin(m) + D.sin(m)
      constant at constant angular velocity \mathbf{w} (or for
21
      configuration 2 at all w).
22
23
24
      A calibration procedure can be carried out to
      determine the values of C(w) for angular velocity
25
      values w (constant in the case of configuration 2)
26
27
      by calculating values of K2(w) with the rotation
28
      axis (OZ) horizontal when C(w) = K2(w).
29
      Thus, for any drilling situation with known angular
30
31
      velocity w, the vector components of the local
      gravity vector {G} can be determined as
32
```

```
1
                                    .....(xxiv)
     GOXY = K1/sin(m)
2
     and
3
     GOZ = (K2(w) - C(w))/cos(m) \qquad .....(xxv)
4
5
     The inclination angle (INC) can then be determined
6
     from
7
8
     sin(INC)/cos(INC) = -GOXY/GOZ ....(xxvi)
9
10
     Azimuth angle
11
12
     When using a rotating fluxgate, the azimuth angle
13
     (AZ) can be determined from a consideration of the
14
     magnetic vector {B}. What follows is applicable to
15
     both configuration 1 and configuration 2.
16
17
     With reference to Fig. 4, it can be shown that
18
19
      BOZ = BV.cos(INC)
20
                  + BN.cos(AZ).sin(INC) ....(xxvii)
21
22
23
      and
24
      BOXY = (BN.cos(AZ).cos(INC)-BV.sin(INC)).cos(HS-MS)
25
                + BN.sin(AZ).sin(HS-MS) ....(xxviii)
26
27
      or, with HS-MS = d a constant,
28
29
      BOXY = (BN.cos(AZ).cos(INC)-BV.sin(INC)).cos(d)
30
                                              ....(xxix)
                 +BN.sin(AZ).sin(d)
31
32
```

```
With {\bf D} the fluxgate datum, the fluxgate output can
1
     be written
2
3
     VB(t) = BOZ.cos(m) + BOXY.sin(m).cos(w.t)
4
                                               .....(xxx)
                + D.sin(m)
5
6
      or
                                               .....(xxxi)
     VB(t) = K1.cos(w.t) + K2
7
     where
8
     K1 = BOXY.sin(m)
9
10
      and
      K2 = BOZ.cos(m) + D.sin(m)
11
                                             .....(xxxii)
         = BOZ.cos(m) + C
12
13
      are constants which can be determined from the
14
      fluxgate output integrations as described above
15
      together with the angle (Magnetic Steering Angle =
16
      MS = w.t) between the axis (OX) and the direction of
17
18
      {BOXY}.
19
      A calibration procedure can be carried out to
20
      determine the value of the constant \boldsymbol{c} by calculating
21
      the value of K2 while rotating about the direction
22
      of the axis (OZ) along which BOZ = 0 when K2 = C.
23
24
      Thus, for any drilling situation the vector
25
      components of the local magnetic field {B} can be
26
      determined as
27
28
                                          .....(xxxiii)
      BOXY = K1/sin(m)
29
30
      and
                                          .....(xxxiv)
      BOZ = (K2-C)/cos(m)
31
```

```
1
     With reference to Fig. 5, the horizontal component
     {BN} of the local magnetic field vector {B} can be
2
     represented by horizontal components {B1} and {B2}
 3
 4
     where
5
     B1 = BOXY.cos(d).cos(INC)
 6
                    + BOZ.sin(INC) ....(xxxv)
 7
 8
     and
                                         ....(xxxvi)
9
     B2 = BOXY.sin(d)
10
11
     The Azimuth Angle (AZ) can then be determined from
12
13
     sin(AZ)/cos(AZ) = -B2/B1 .....(xxxvii)
14
15
     Also, the horizontal component of the local magnetic
16
     field can be determined from
17
     BN = (B1^2 + B2^2)^{3/2}
18
                                   .....(xxxviii)
19
      and the vertical component of the local magnetic
20
      field can be determined from
2.1
22
     BV = BOZ.cos(INC)
23
24
                - BOXY.cos(d).sin(INC) ....(xxxix)
25
26
     Earth's rotation vector
27
2.8
     Where it is not practicable to use a magnetic
29
      fluxgate, this may be replaced by a rate gyro as
30
      sensor.
```

```
With reference to Fig. 6, if the geographic latitude
1
     at the drilling location is (LAT) then the vertical
     component of the earth's Rotation Vector {RE} is
3
4
                                 ....(x1)
5
     RV = -RE.sin(LAT)
     and the horizontal component is
6
     RN = RE.cos(LAT)
7
                                  ....(xli)
8
9
     The magnitude of the cross-axis rate vector {ROXY}
     can be shown to be
10
11
     ROXY = (RN.cos(GAZ).cos(INC)-RV.sin(INC)).cos(d)
12
               + RN.sin(GAZ)sin(d) .....(xlii)
13
14
     where (GAZ) is the gyro azimuth angle and
15
     d = HS - GS is constant.
16
17
     Since RN, RV, d and INC are known and ROXY can be
18
     derived as discussed below, (GAZ) can be determined.
19
20
21
     With the particular configuration where the rate
     gyro sensing axis is perpendicular to the drill
22
     string rotation axis (OZ), the rate gyro output can
23
24
     be written
25
     VG(t) = ROXY.cos(w.t) + D .....(xliii)
26
27
28
     where D is the rate gyro datum, or
29
     VG(t) = K1.\cos(w.t) + K2 \qquad \dots (xliv)
30
```

where the constant K1 = ROXY can be determined from 1 2 the rate gyro output integrations as described above together with the Gyro Steering Angle GS = w.t 3 between (OX) and the direction of {ROXY}. 4 The variation in the Rate Gyro Datum makes it 7 difficult to achieve satisfactory datum calibration 8 in all circumstances. It is unlikely that Gyro Azimuth measurements should be attempted at high 9 10 inclination angles. The use of the rate gyro is 11 most likely with near-vertical boreholes in 12 locations where magnetic azimuth measurements are 13 unreliable (such as close to rigs) and the Gyro 14 Azimuth GAZ is approximately equal to the angle d. 15 16 The present invention thus makes possible the measurement of a number of borehole-related 17 parameters during rotation of a drillstring and 18 19 using a reduced number of sensors. Modifications may be made to the foregoing embodiments within the 20

scope of the present invention.